

Jeopardy!

Linear Fcns	Quad. Fcns	Quad. Models	Quad. Ineq.	Polyn'1 Fcns & Models	Props of Rat. Fcns	Graph of Rat. Fcns	Polyn'1 & Rat. Ineq.
<u>100</u>	<u>100</u>	<u>100</u>	<u>100</u>	<u>100</u>	<u>100</u>	<u>100</u>	<u>100</u>
<u>200</u>	<u>200</u>	<u>200</u>	<u>200</u>	<u>200</u>	<u>200</u>	<u>200</u>	<u>200</u>
<u>300</u>	<u>300</u>	<u>300</u>	<u>300</u>	<u>300</u>	<u>300</u>	<u>300</u>	<u>300</u>
<u>400</u>	<u>400</u>	<u>400</u>	<u>400</u>	<u>400</u>	<u>400</u>	<u>400</u>	<u>400</u>
<u>500</u>	<u>500</u>	<u>500</u>	<u>500</u>	<u>500</u>	<u>500</u>	<u>500</u>	<u>500</u>

Grab Bag

100

200

300

400

500

- Determine the slope, y -intercept, where the function is increasing and decreasing and graph the function:

$$f(x) = -\frac{x}{3} + 1$$

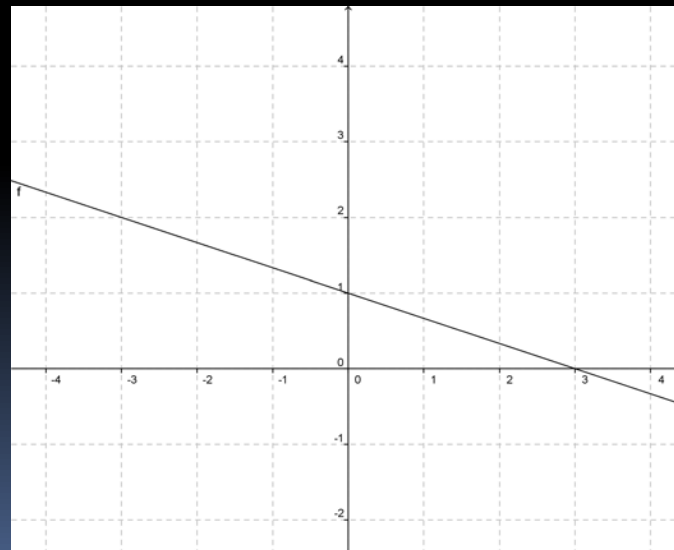
Linear Fcns

100

$$\text{Slope} = -\frac{1}{3}$$

y-intercept= 1

Decreasing on whole real line, Increasing nowhere



Determine the slope, y-intercept, where the function is increasing and decreasing and graph the function:

$$f(x) = \frac{4}{5}x - 6$$

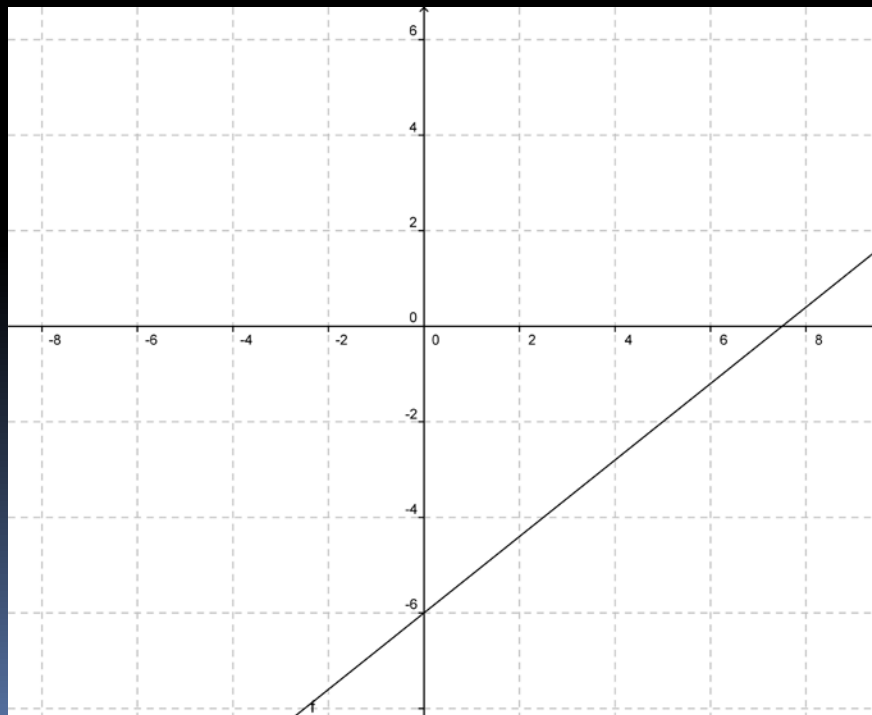
Linear Fcns

200

$$\text{Slope} = \frac{4}{5}$$

y-intercept= -6

Increasing on whole real line, Decreasing nowhere



Determine the slope, y -intercept, where the function is increasing and decreasing and graph the function:

$$h(x) = 4$$

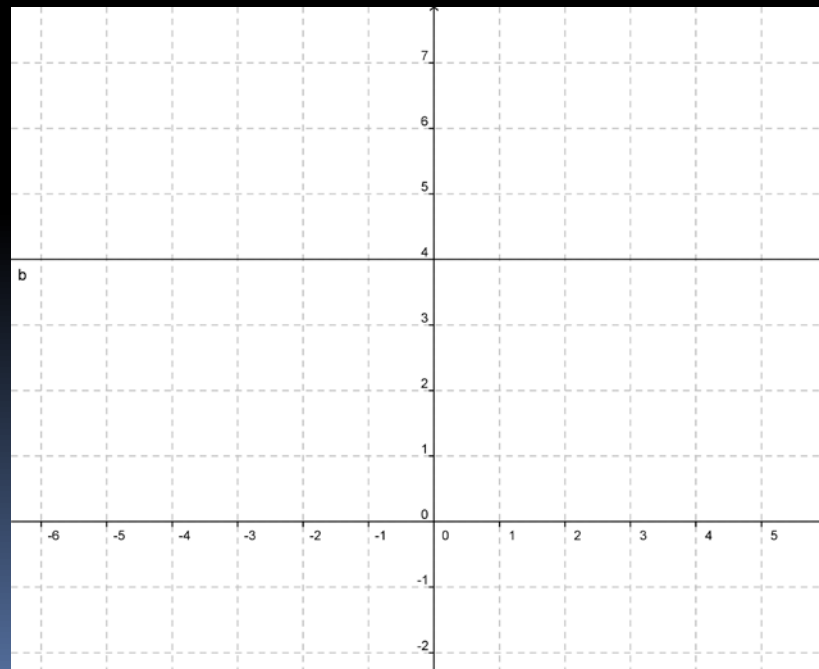
Linear Fcns

300

Slope = 0

y-intercept = 4

Increasing/Decreasing nowhere



Determine the slope, y -intercept, where the function is increasing and decreasing and graph the function:

$$3y + 12 = 6x - 3$$

Linear Fcns

400

$$3y + 12 = 6x - 3$$

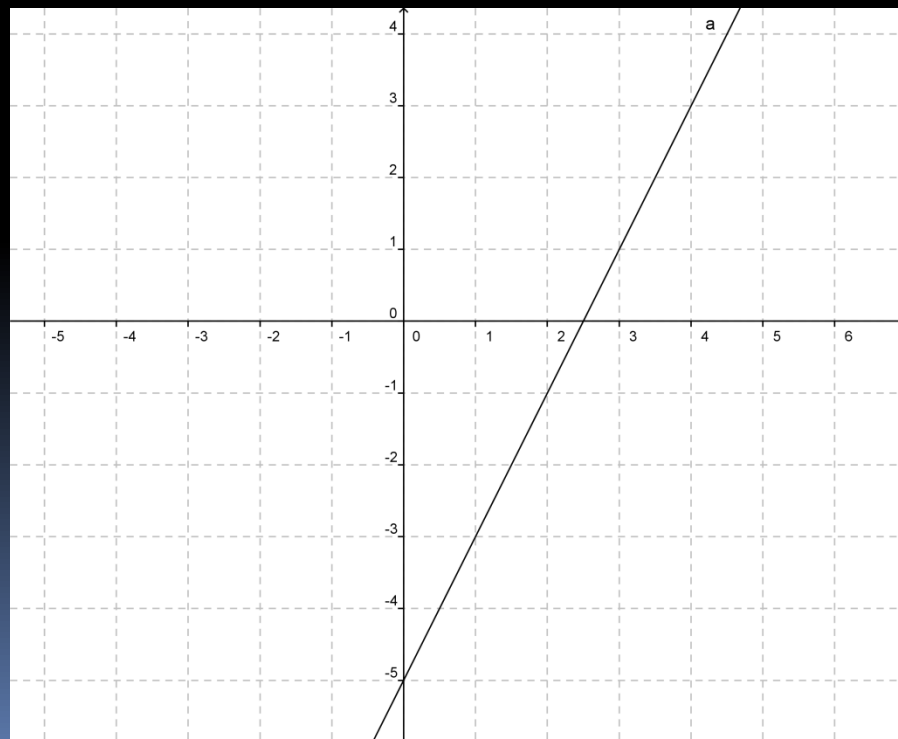
$$3y = 6x - 15$$

$$y = 2x - 5$$

Slope = 2

y-intercept = -5

Increasing on whole real line, Decreasing nowhere



Marissa must decide between one of two companies as her long-distance phone provider. Company A charges a monthly fee of \$7.00 plus \$0.06 per minute while Company B does not have a monthly fee, but charges \$0.08 per minute.

- (a) Find a linear function that relates cost, C , to total minutes on the phone, x , for each company.
- (b) Determine the number of minutes x for which the bill from Company A would equal the bill from Company B.
- (c) Over what interval of minutes x will the bill from Company B be less than the bill from Company A?

Linear Fcns

500

(a) $C_A(x) = 7 + 0.06x$
 $C_B(x) = 0.08x$

(b) $7 + 0.06x = 0.08x$
 $7 = 0.02x$
 $350 = x$
 $x = 350 \text{ min}$

(c) $0 \leq x \leq 350$

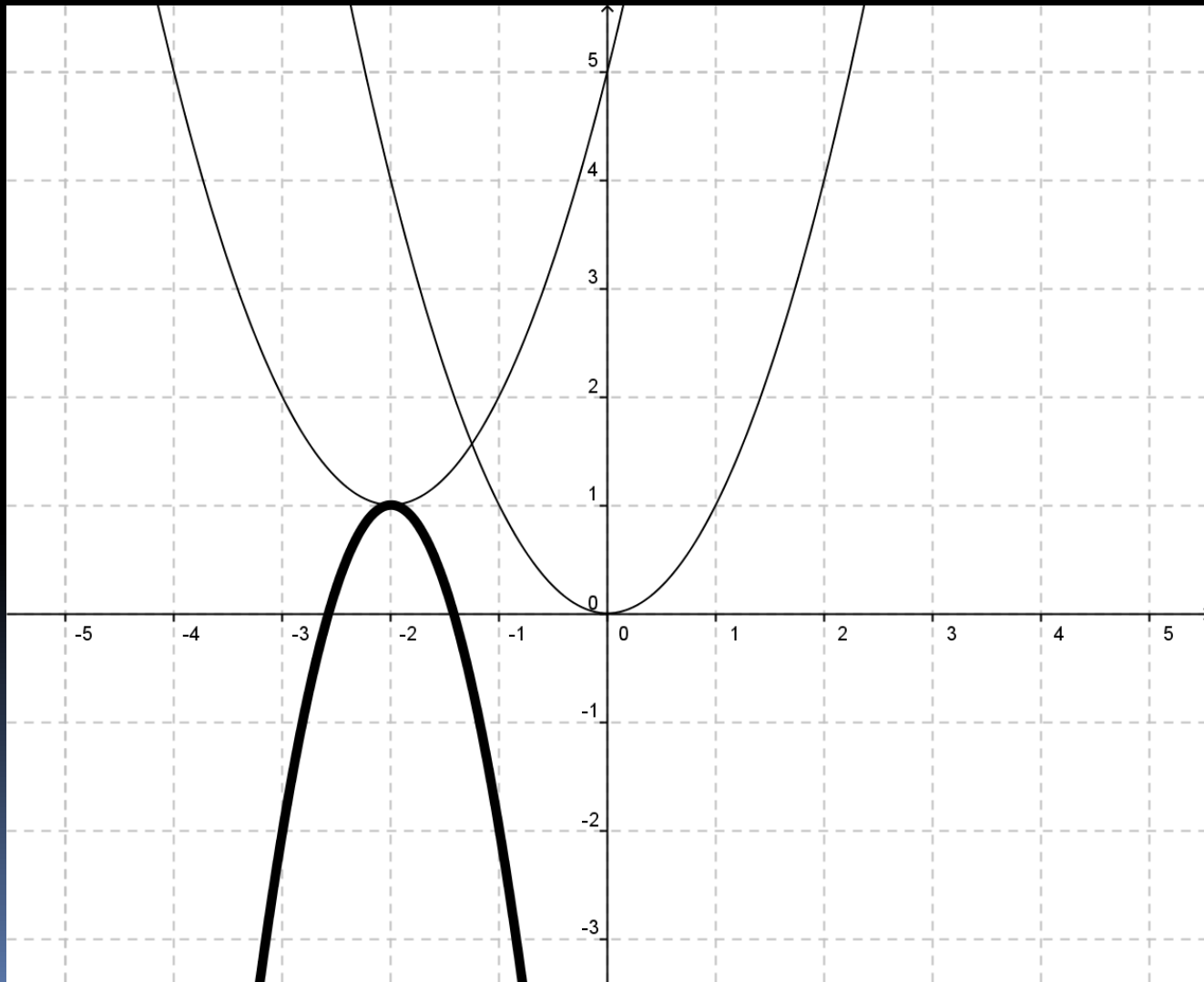
Graph using transformations

$$f(x) = -3(x + 2)^2 + 1$$

Quad Fcns

100

(Bold function is final answer)



Graph by finding vertex, axis of symmetry, and any intercepts

$$f(x) = 9x^2 - 6x + 3$$

Quad Fcns

200

$$f(x) = 9x^2 - 6x + 3$$

Vertex:

$$\frac{-b}{2a} = -\frac{-6}{18} = \frac{1}{3}$$

$$f\left(\frac{-b}{2a}\right) = f\left(\frac{1}{3}\right) = 2$$

$$\left(\frac{1}{3}, 2\right)$$

Axis of Symmetry:

$$x = \frac{1}{3}$$

Intercepts:

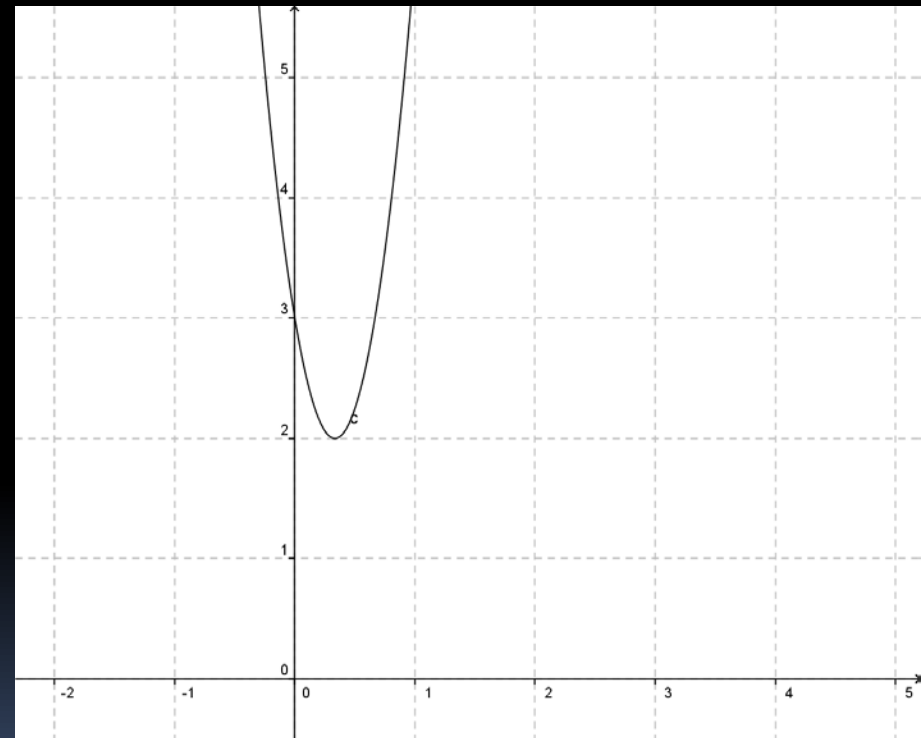
x:

$$y = 0 \Rightarrow 0 = 9x^2 - 6x + 3$$

$$\frac{6 \pm \sqrt{36 - 108}}{12} \Rightarrow \text{nonreal}$$

y:

$$x = 0 \Rightarrow f(x) = y = 3 \Rightarrow (0, 3)$$



Graph by finding vertex, axis of symmetry, and any intercepts

$$y = -4x^2 + 4x$$

Quad Fcns

300

Vertex:

$$\frac{-b}{2a} = -\frac{4}{-8} = \frac{1}{2}$$

$$f\left(\frac{-b}{2a}\right) = f\left(\frac{1}{2}\right) = 1$$

$$\left(\frac{1}{2}, 1\right)$$

Axis of Symmetry:

$$x = \frac{1}{2}$$

Intercepts:

x:

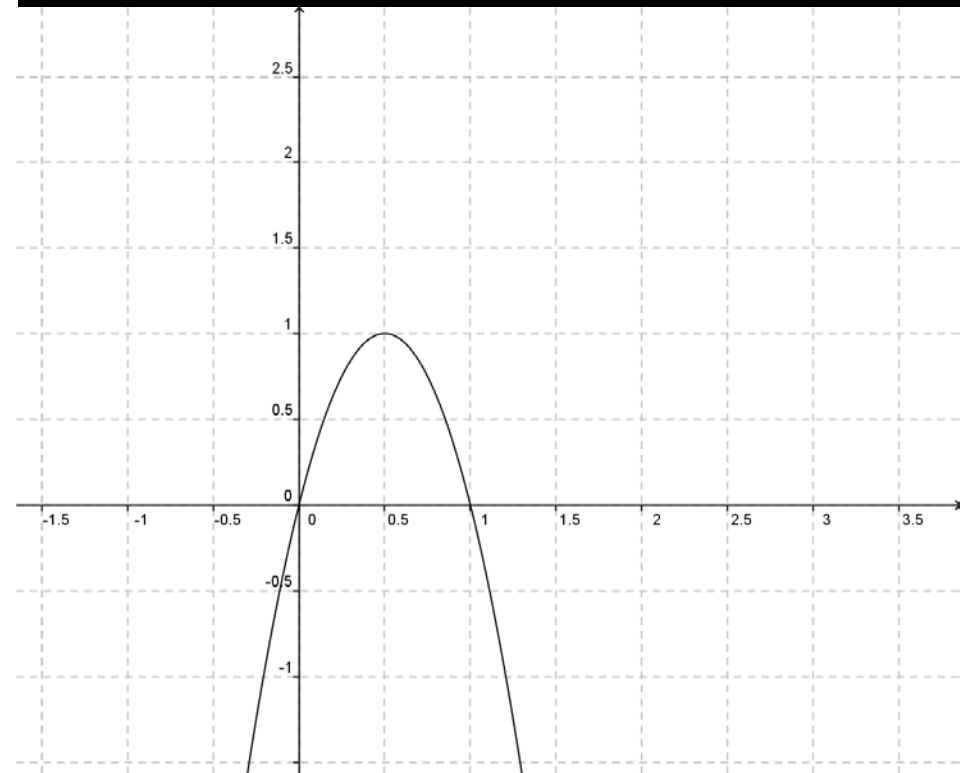
$$y = 0 \Rightarrow 0 = -4x^2 + 4x$$

$$0 = x(-x + 1)$$

$$x = 0, 1 \Rightarrow (0, 0), (1, 0)$$

y:

$$x = 0 \Rightarrow f(x) = y = 0 \Rightarrow (0, 0)$$



Determine whether the given quadratic has a max or min value and find its value.

$$y = 2x^2 + 8x + 5$$

Quad Fcns

400

$$y = 2x^2 + 8x + 5$$

The function will have a min value as the coefficient of the squared term is positive, meaning the parabola opens up. (To verify, you may graph and/or determine where the function is increasing and decreasing). The min value will be located at the vertex:

Vertex

$$\frac{-b}{2a} = \frac{-8}{4} = -2$$

$$f\left(\frac{-b}{2a}\right) = f(-2) = -3$$

$$(-2, -3)$$

Determine whether the given quadratic has a max or min value and find its value.

$$f(x) = -x^2 - 10x - 3$$

Quad Fcns

500

$$f(x) = -x^2 - 10x - 3$$

The function will have a max value as the coefficient of the squared term is negative, meaning the parabola opens down. (To verify, you may graph and/or determine where the function is increasing and decreasing). The max value will be located at the vertex:

Vertex:

$$\frac{-b}{2a} = -\frac{-10}{-2} = -5$$

$$f(-5) = 22$$

$$(5, 22)$$

The price p (in dollars) and the quantity x sold of a certain product obey the demand equation

$$p = -\frac{1}{10}x + 150, p \in [0, 1500]$$

- (a) Express the revenue R as a function of x .
- (b) What quantity x maximizes the revenue?

Quad Models

100

$$p = -\frac{1}{10}x + 150, p \in [0, 1500]$$

(a) $R = xp = x\left(-\frac{1}{10}x + 150\right) = -\frac{1}{10}x^2 + 150x$

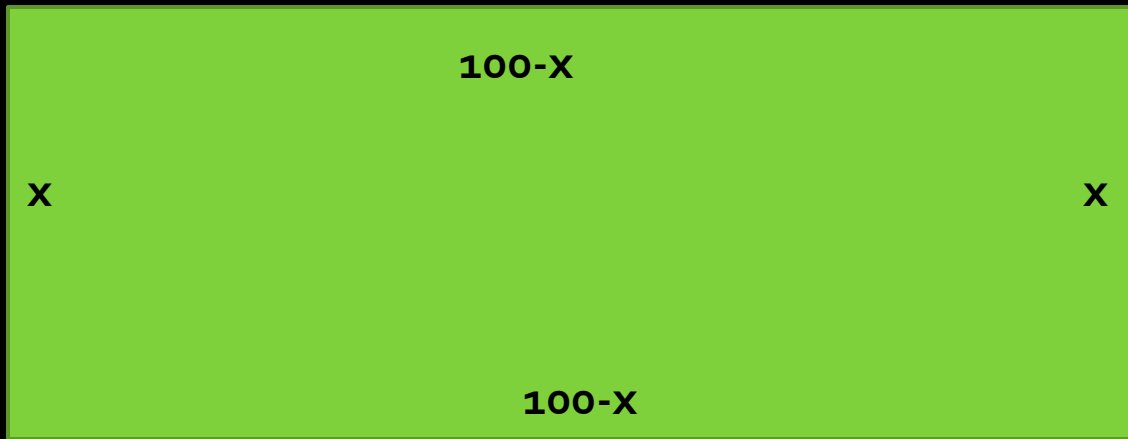
(b) *Vertex*

$$-\frac{b}{2a} = -\frac{150}{2\left(-\frac{1}{10}\right)} = 750 = x$$

A landscape engineer has 200ft of border to enclose a rectangular pond. What dimensions will result in the largest pond?

Quad Models

200



$$P = 2x + 2y = 200$$

$$\Rightarrow y = 100 - x$$

$$A = xy = x(100 - x) = 100x - x^2$$

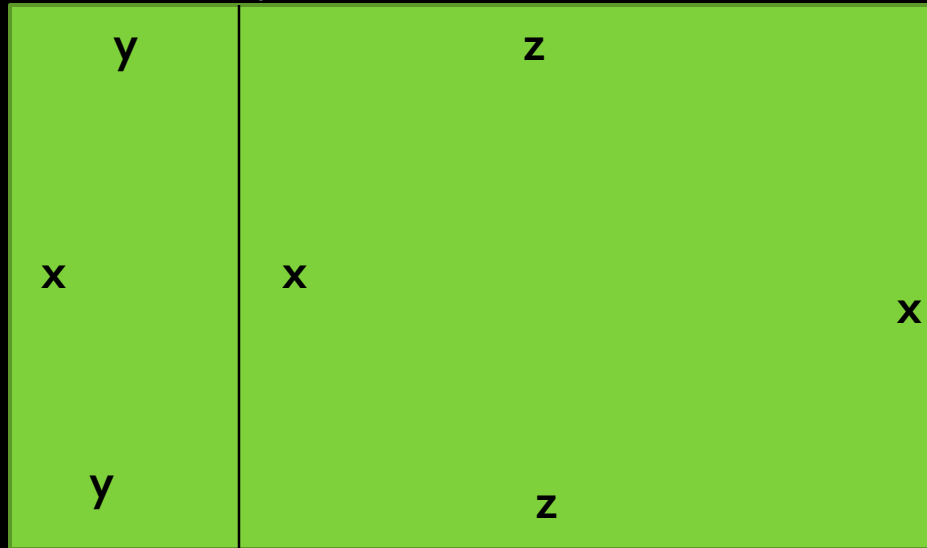
$$\text{Vertex} = -\frac{b}{2a} = -\frac{100}{-2} = 50 \text{ ft} = x$$

$$\Rightarrow y = 50 \text{ ft}$$

A farmer with 10,000 m of fencing wants to enclose a rectangular field and then divide it into two plots with a fence parallel to one of the sides. What is the largest area that can be enclosed?

Quad Models

300



$$P = 3x + 2y + 2z = 10,000$$

$$w = y + z$$

$$w = \frac{10,000 - 3x}{2}$$

$$A = xw = x\left(\frac{10,000 - 3x}{2}\right) = \frac{10,000x - 3x^2}{2}$$

$$\text{Vertex} = -\frac{b}{2a} = -\frac{10,000}{2\left(\frac{-3}{2}\right)} = 3,333.33m = x$$

$$A_{\max} = \frac{10,000(3,333.33) - 3(3,333.33)^2}{2}$$

The marginal cost C of a company manufacturing x golf clubs may be expressed by the quadratic function

$$C(x) = 4.9x^2 - 617.4x + 19,600$$

- (a) How many clubs should be manufactured to minimize the marginal cost?
- (b) At this level of production, what is the marginal cost?

Quad Models

400

$$C(x) = 4.9x^2 - 617.4x + 19,600$$

(a) Vertex = $\frac{617.4}{9.8} = 63$

(b) $C(63) = 4.9(63)^2 - 617.4(63) + 19,600 = \151.90

- The price p (in dollars) and the quantity x sold of a certain product obey the demand equation

$$x = -20p + 500, p \in [0, 25]$$

- (a) express the revenue R as a function of x
- (b) What is the revenue if 20 units are sold?
- (c) What quantity x maximizes revenue? What is the maximum revenue?

Quad Models

500

$$x = -20p + 500, p \in [0, 25]$$

(a)

$$p = \frac{x - 500}{-20}$$

$$R(x) = xp = x\left(\frac{x - 500}{-20}\right) = 25x - \frac{x^2}{20}$$

(b)

$$R(20) = 25(20) - \frac{20^2}{20} = 500 - 20 = \$480$$

(c)

$$-\frac{b}{2a} = -\frac{25}{\frac{-2}{20}} = 250$$

$$R(250) = 25(250) - \frac{250^2}{20} = \$3125$$

Solve

$$x^2 + 6x - 16 < 0$$

Quad Ineq

100

$$x^2 + 6x - 16 < 0$$

$$x^2 + 6x + 9 < 25$$

$$(x + 3)^2 < 25$$

$$x + 3 < 5, x + 3 > -5$$

$$x < 2, x > -8$$

$$-8 < x < 2$$

OR

$$\{x \mid -8 < x < 2\}$$

OR

$$(-8, 2)$$

Solve

$$3x^2 - 2x - 1 \geq 0$$

Quad Ineq

200

$$3x^2 - 2x - 1 \geq 0$$

$$3\left(x^2 - \frac{2}{3}x\right) \geq 1$$

$$3\left(x^2 - \frac{2}{3}x + \frac{1}{9}\right) \geq \frac{4}{3}$$

$$\left(x - \frac{1}{3}\right)^2 \geq \frac{4}{9}$$

$$x - \frac{1}{3} \geq \frac{2}{3}, x - \frac{1}{3} \leq -\frac{2}{3}$$

$$x \geq 1, x \leq -\frac{1}{3}$$

Solve

$$3x^2 \geq 14x + 5$$

Quad Ineq

300

$$3x^2 \geq 14x + 5$$

$$3\left(x^2 - \frac{14}{3}x\right) \geq 5$$

$$3\left(x^2 - \frac{14}{3}x + \frac{49}{9}\right) \geq \frac{64}{3}$$

$$\left(x - \frac{7}{3}\right)^2 \geq \frac{64}{9}$$

$$x - \frac{7}{3} \geq \frac{8}{3}, x - \frac{7}{3} \leq -\frac{8}{3}$$

$$x \geq 5, x \leq -\frac{1}{3}$$

Solve

$$4x^2 < 13x - 3$$

Quad Ineq

400

$$4x^2 < 13x - 3$$

$$4x^2 - 13x < -3$$

$$4\left(x^2 - \frac{13}{4}x + \frac{169}{64}\right) < \frac{121}{16}$$

$$\left(x - \frac{13}{8}\right)^2 < \frac{121}{64}$$

$$x - \frac{13}{8} < \frac{11}{8}, x - \frac{13}{8} > -\frac{11}{8}$$

$$x < 3, x > \frac{1}{4} \Rightarrow \frac{1}{4} < x < 3$$

Solve

$$7x + 15 > 2x^2$$

Quad Ineq

500

$$7x + 15 > 2x^2$$

$$15 > 2\left(x^2 - \frac{7}{2}x\right)$$

$$\frac{169}{8} > 2\left(x^2 - \frac{7}{2}x + \frac{49}{16}\right)$$

$$\frac{169}{16} > \left(x - \frac{7}{4}\right)^2$$

$$\frac{13}{4} > x - \frac{7}{4}, -\frac{13}{4} < x - \frac{7}{4}$$

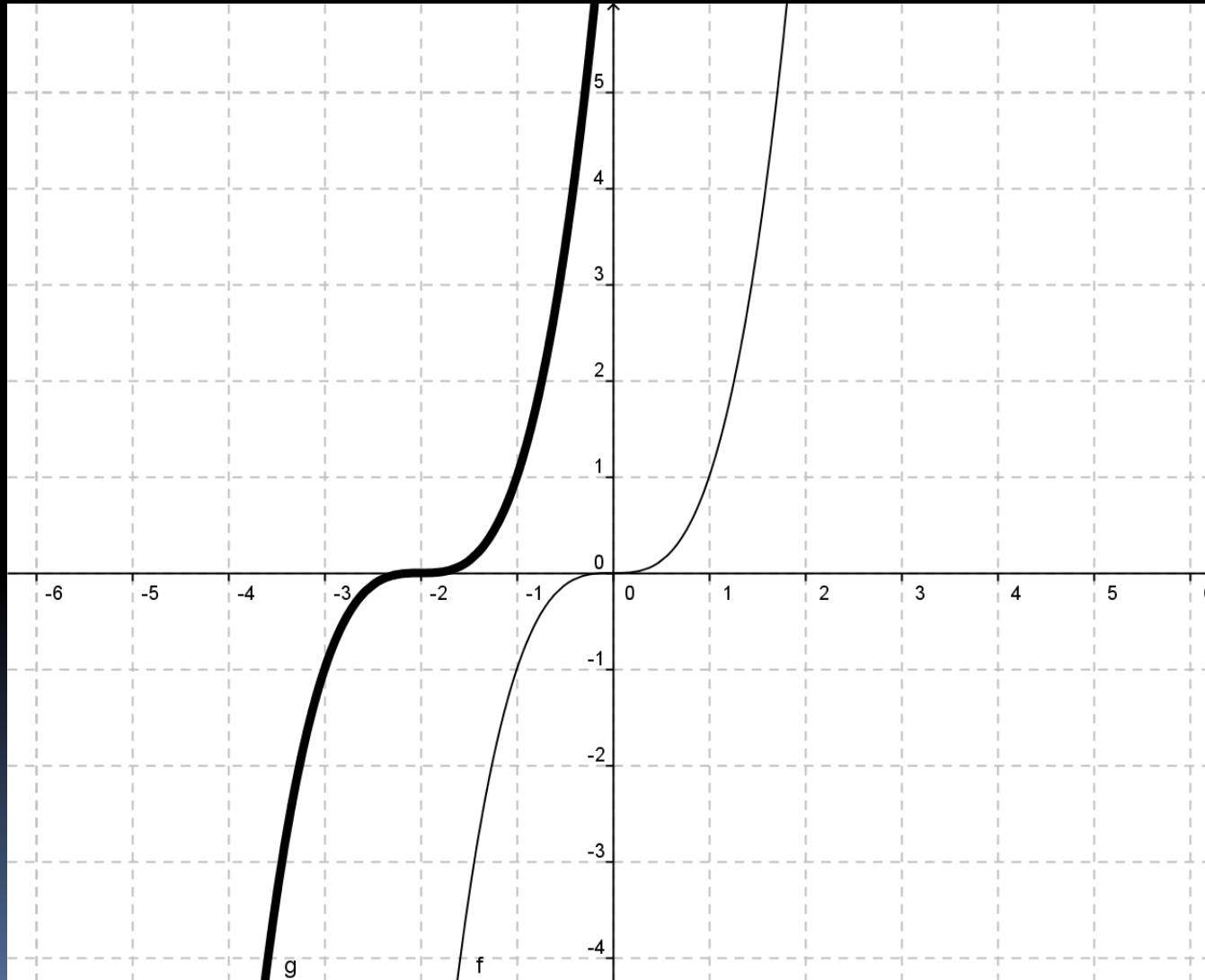
$$5 > x, -\frac{3}{2} < x \implies -\frac{3}{2} < x < 5$$

Graph the function using transformations.
Show all stages (on same graph)

$$f(x) = (x + 2)^3$$

Polyn'1 Fcns & Models

100

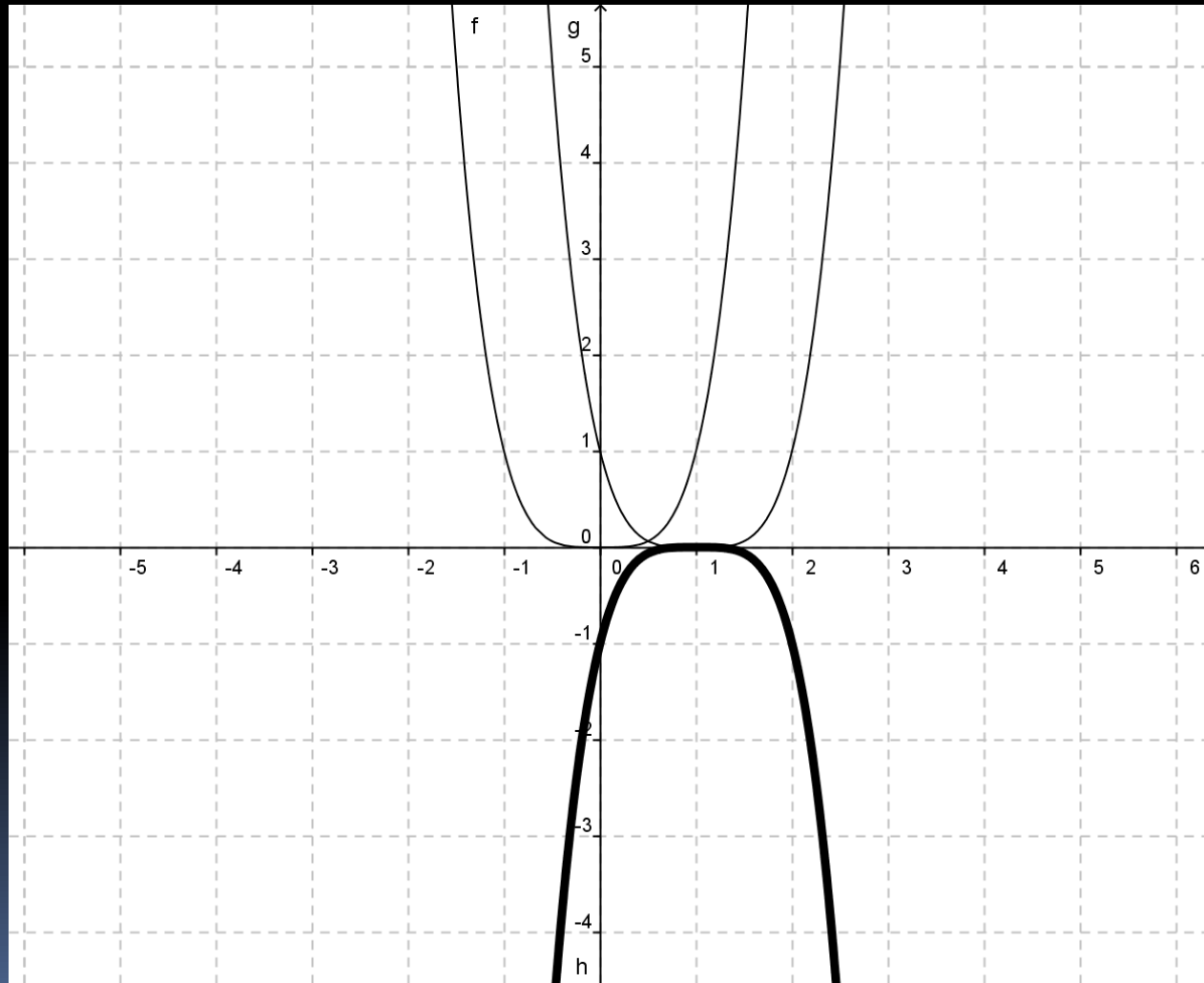


Graph the function using transformations.
Show all stages (on same graph)

$$f(x) = -(x-1)^4$$

Polyn'1 Fcns & Models

200



Find the intercepts, where the function touches or crosses the x-axis, and determine the end behavior of the function.

$$f(x) = 4(x-1)^3(x+3)^2$$

Polyn'1 Fcns & Models

300

$$f(x) = 4(x-1)^3(x+3)^2$$

Intercepts:

x: x=1, x=-3

y: y=-36

Crosses at x=1 due to odd multiplicity, Touches at x=-3 due to even multiplicity

For $x \gg 0$, $f(x)$ goes to infinity, for $x \ll 0$, $f(x)$ goes to negative infinity

Find the intercepts, where the function touches or crosses the x-axis, and determine the end behavior of the function.

$$g(x) = -2x^3 + 4x^2$$

Polyn'1 Fcns & Models

400

$$g(x) = -2x^3 + 4x^2 = -2x^2(x - 2)$$

Intercepts:

x: x=0, x=2

y:y=0

Crosses at x=2 due to odd multiplicity, Touches at x=0 due to even multiplicity

For $x \gg 0$, $f(x)$ goes to negative infinity, for $x \ll 0$, $f(x)$ goes to infinity

Find the intercepts, where the function touches or crosses the x-axis, the number of turning points, and determine the end behavior of the function. Sketch the function.

$$h(x) = x(x + 2)(x + 4)$$

Polyn'1 Fcns & Models

500

$$h(x) = x(x + 2)(x + 4)$$

Intercepts:

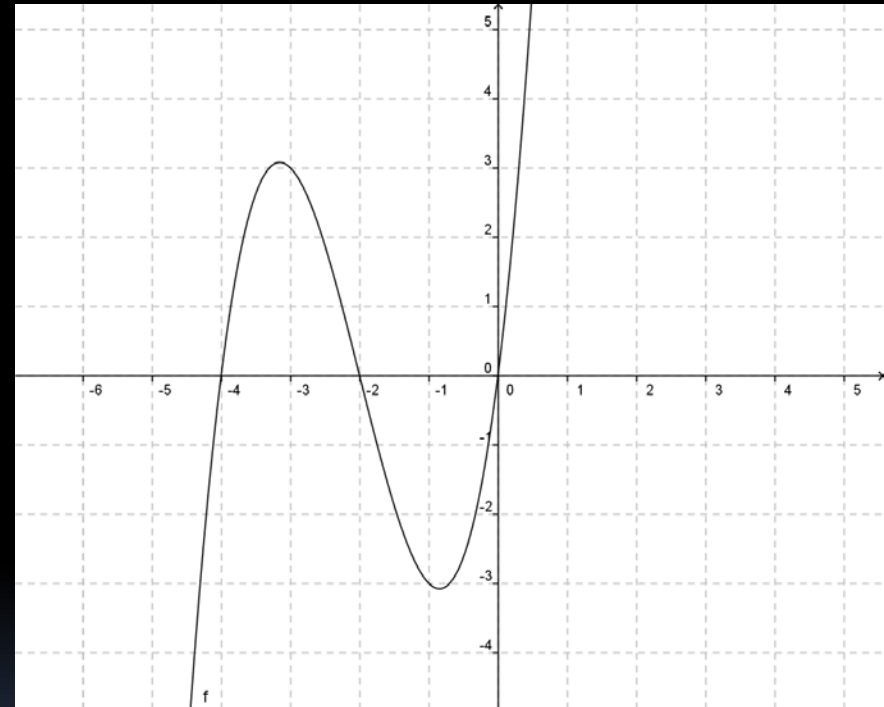
x: $x=0$, $x=-2$, $x=-4$

y: $y=0$

Crosses at all x intercepts due to odd multiplicity

Number of Turning Points: 2

For $x \gg 0$, $f(x)$ goes to infinity, for $x \ll 0$, $f(x)$ goes to negative infinity



Props of Rat. Fcns

100

Find the domain and any horizontal, vertical, and oblique asymptotes

$$R(x) = \frac{x+2}{x^2-9}$$

Props of Rat. Fcns

100

$$R(x) = \frac{x+2}{x^2-9} = \frac{x+2}{(x-3)(x+3)}$$

Domain: All reals except $x=3, x=-3$

VA: $x=3, x=-3$

HA: $x=0$ since (degree numerator) < (degree denominator)

OA: none

Props of Rat. Fcns

200

Find the domain and any horizontal, vertical, and oblique asymptotes

$$R(x) = \frac{x^2 + 4}{x - 2}$$

Props of Rat. Fcns

200

$$R(x) = \frac{x^2 + 4}{x - 2}$$

Domain: All reals except $x=2$

VA: $x=2$

HA: none since (degree numerator) $>$ (degree denominator)

OA: $y=x+2$ after long division

Props of Rat. Fcns

300

Find the domain and any horizontal, vertical, and oblique asymptotes

$$R(x) = \frac{x^2 + 3x + 2}{(x + 2)^2}$$

Props of Rat. Fcns

300

$$R(x) = \frac{x^2 + 3x + 2}{(x + 2)^2} = \frac{(x + 1)(x + 2)}{(x + 2)^2} = \frac{x + 1}{x + 2}$$

Domain: All reals except $x = -2$

VA: $x = -2$

HA: $x = 1$ since (degree numerator)=(degree denominator), look at coefficients of the highest degree in each.

OA: none

Props of Rat. Fcns

400

Find the domain and any horizontal, vertical, and oblique asymptotes

$$R(x) = \frac{x^3}{x^3 - 1}$$

Props of Rat. Fcns

400

$$R(x) = \frac{x^3}{x^3 - 1} = \frac{x^3}{(x-1)(x^2 + x - 1)}$$

Domain: All reals except $x=1$ (the quadratic term results in nonreal values for x)

VA: $x=1$

HA: $x=1$ since (degree numerator)=(degree denominator), we look at the coefficients of the highest degree term in each.

OA: none

Props of Rat. Fcns

500

Find the domain and any horizontal, vertical, and oblique asymptotes

$$G(x) = \frac{x^3 - 1}{x - x^2}$$

Props of Rat. Fcns

500

$$G(x) = \frac{x^3 - 1}{x - x^2} = \frac{(x-1)(x^2 + x - 1)}{x(1-x)} = \frac{(x-1)(x^2 + x - 1)}{-x(x-1)} = -\frac{(x^2 + x - 1)}{x}$$

Domain: All reals except $x=0, x=1$, hole at $x=1$

VA: $x=0$

HA: none since (degree numerator) > (degree denominator)

OA: $y=-x-1$ after long division

Graphs of Rat. Fcns

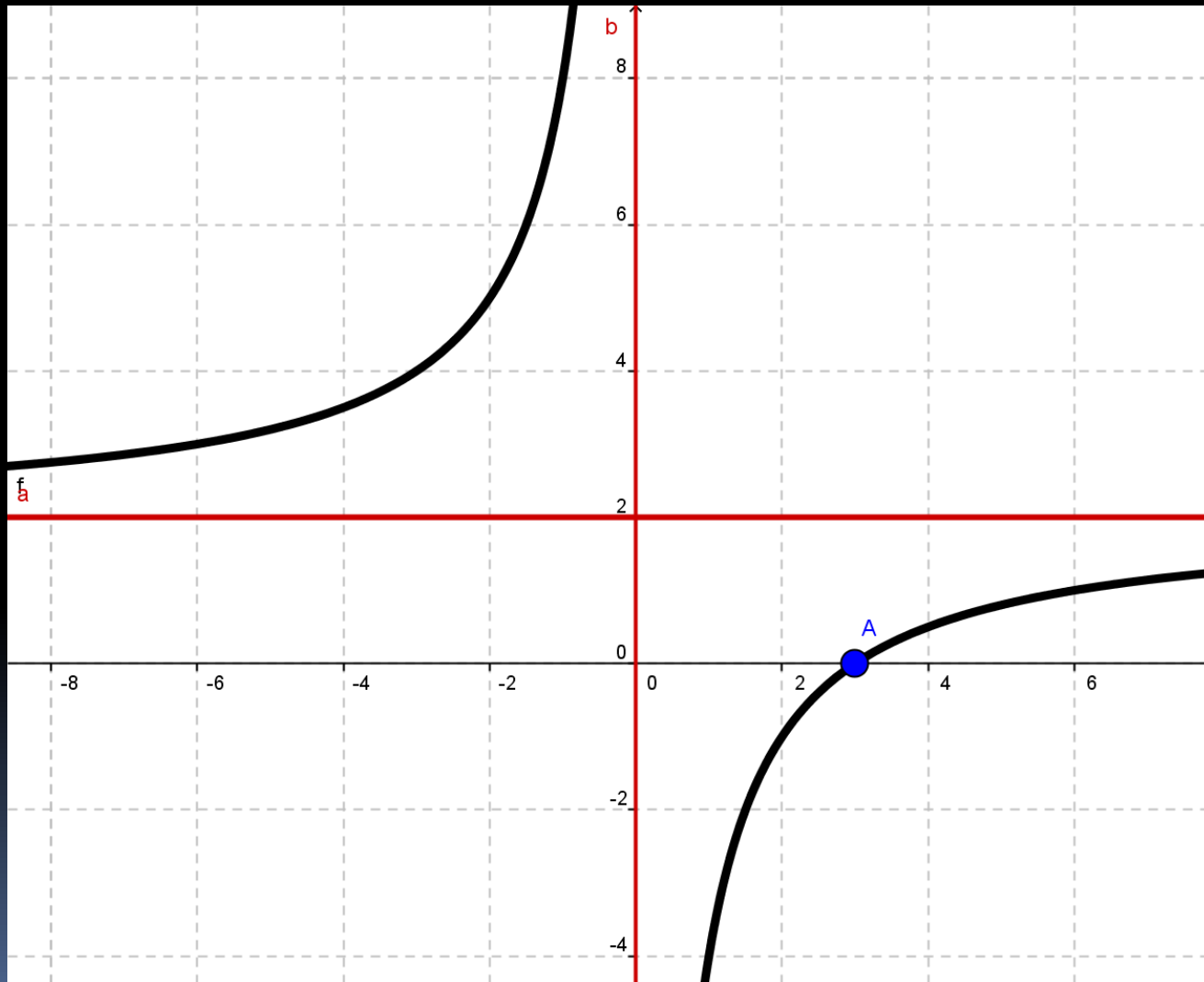
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Go through the seven step process to obtain the graph of the function:

$$R(x) = \frac{2x - 6}{x}$$

Graphs of Rat. Fcns

100



Graphs of Rat. Fcns

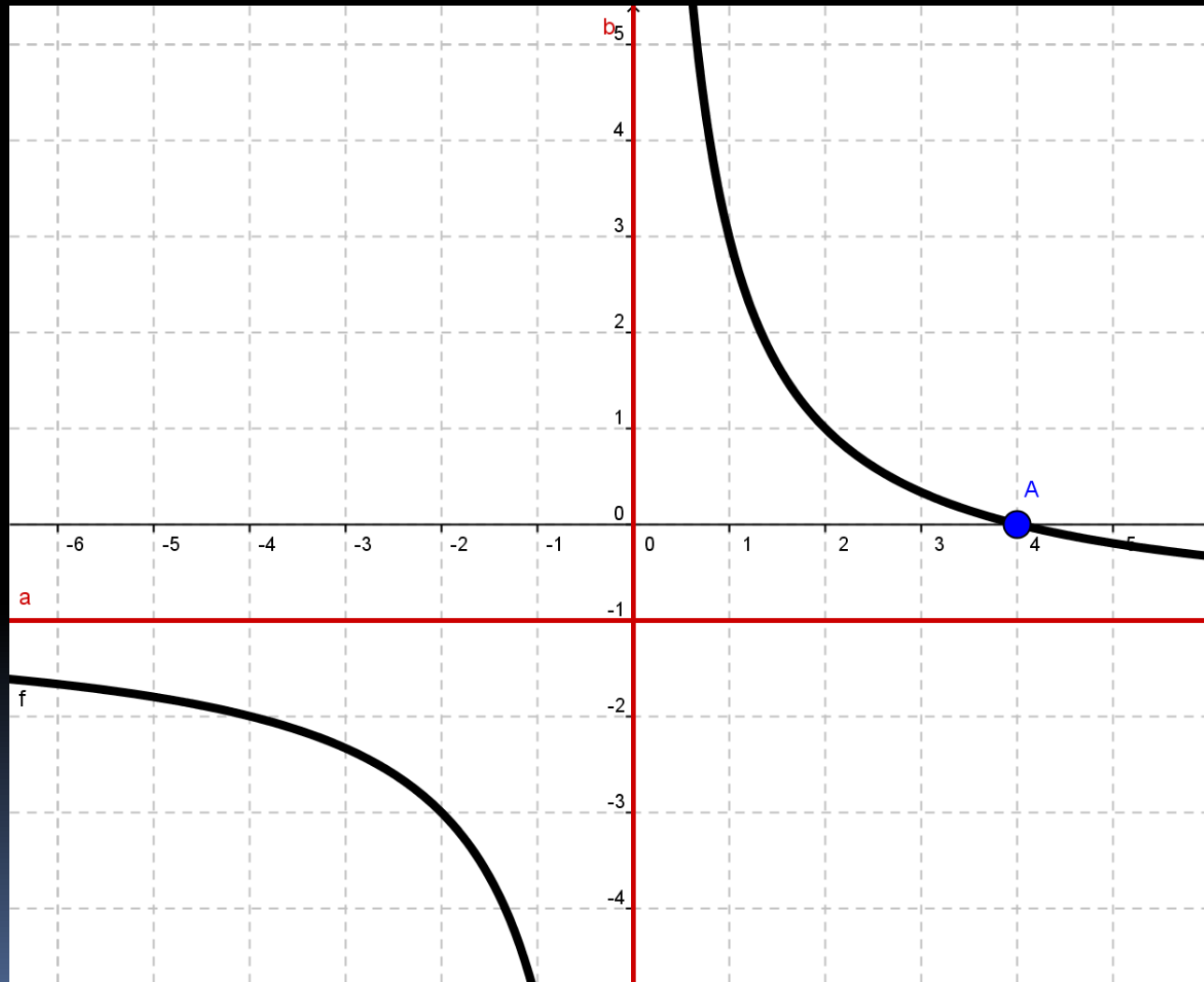
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Go through the seven step process to obtain the graph of the function:

$$R(x) = \frac{4 - x}{x}$$

Graphs of Rat. Fcns

200

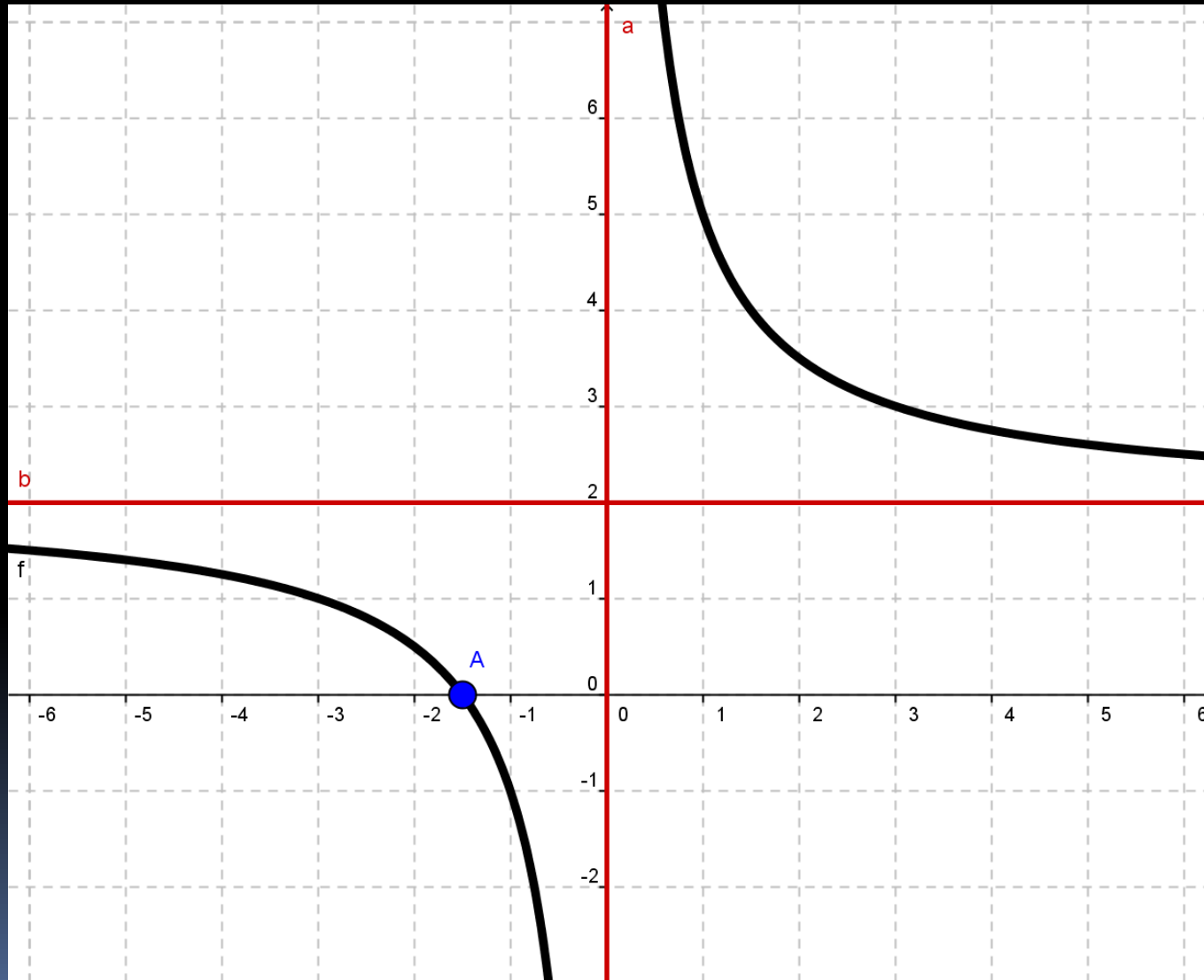


Go through the seven step process to obtain the graph of the function:

$$R(x) = \frac{2x^2 - 7x - 15}{x^2 - 5x}$$

Graphs of Rat. Fcns

300

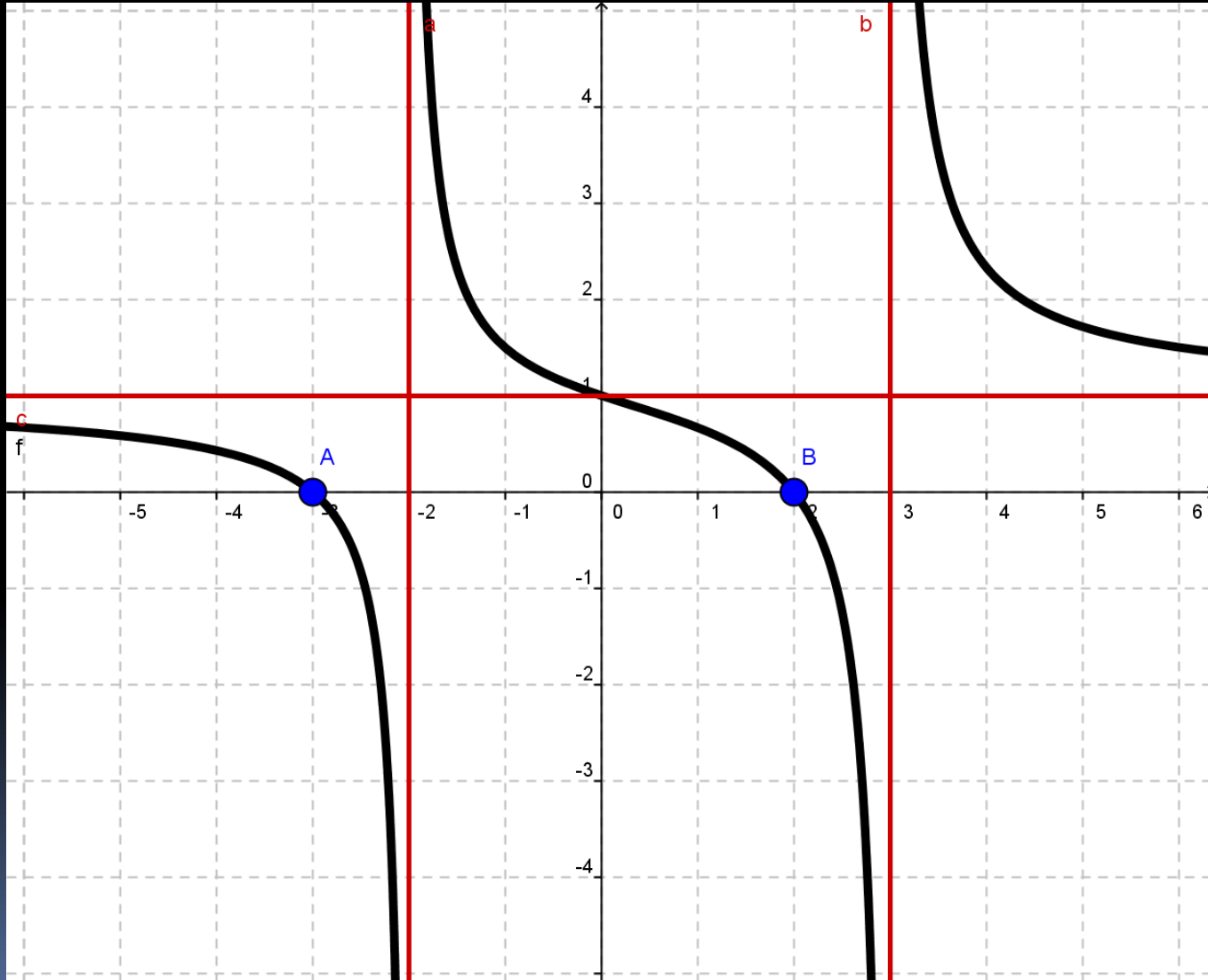


Go through the seven step process to obtain the graph of the function:

$$R(x) = \frac{x^2 + x - 6}{x^2 - x - 6}$$

Graphs of Rat. Fcns

400



Graphs of Rat. Fcns

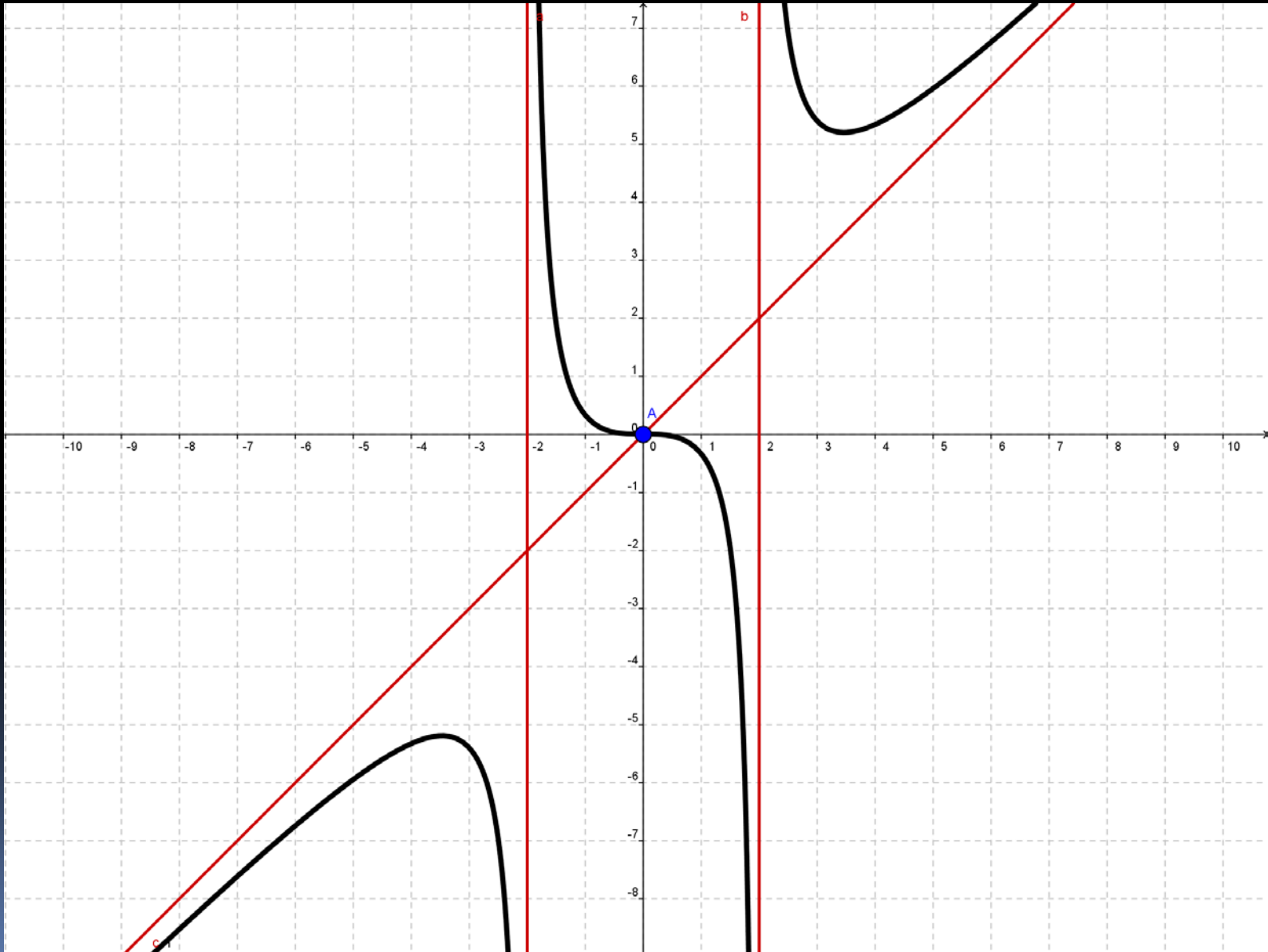
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Go through the seven step process to obtain the graph of the function:

$$R(x) = \frac{x^3}{x^2 - 4}$$

Graphs of Rat. Fcns

500



Solve

$$\frac{2x-6}{1-x} < 2$$

$$\frac{2x-6}{1-x} < 2 \Rightarrow x \neq 1$$

$$2x-6 < 2-2x$$

$$4x < 8$$

$$x < 2$$

$$(-\infty, 1) \cup (1, 2)$$

Solve

$$\frac{1}{x} - 2 > x$$

$$\frac{1}{x} - 2 > x$$

$$1 - 2x > x^2$$

$$0 > x^2 + 2x - 1$$

$$0 > (x - 1)^2$$

$$0 > x - 1, 0 < x - 1$$

$$x < 1, x > 1 \Rightarrow x \in \mathbb{R}$$

Solve & Graph the solution set.

$$\frac{(x-2)(x-1)}{x-3} \geq 0$$

Polyn'1 & Rat. Ineq

300

$$\frac{(x-2)(x-1)}{x-3} \geq 0$$

Critical pts: 3, 2, 1

Intervals:

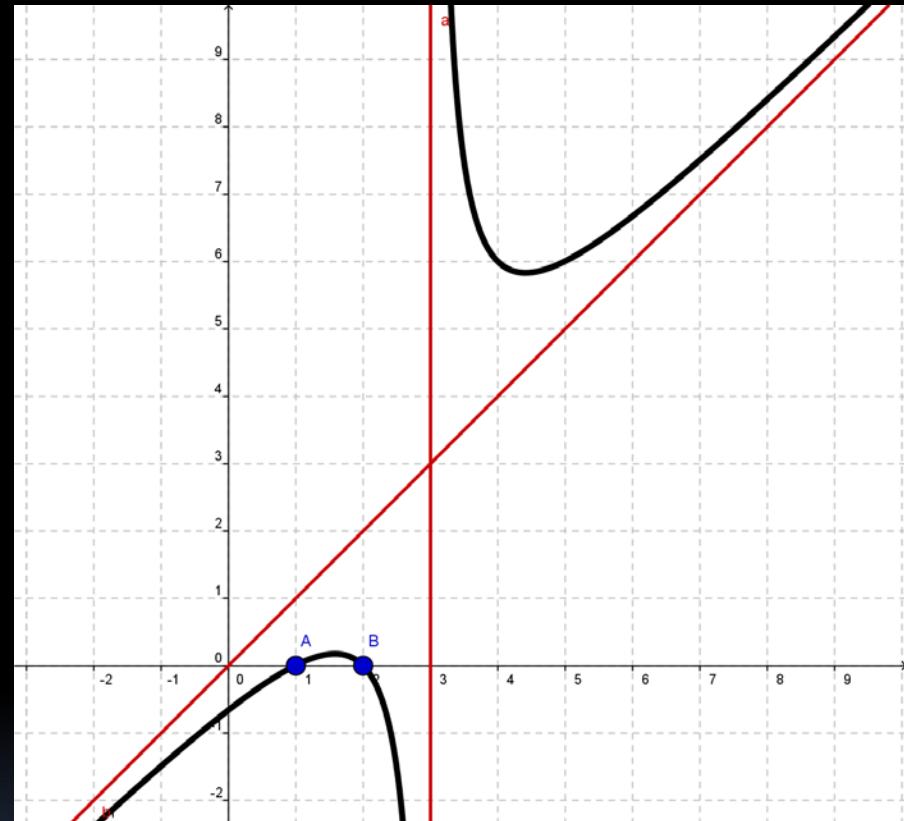
$$(-\infty, 1) \Rightarrow 0 \Rightarrow \leq 0$$

$$(1, 2) \Rightarrow 1.5 \Rightarrow \geq 0$$

$$(2, 3) \Rightarrow 2.5 \Rightarrow \leq 0$$

$$(3, \infty) \Rightarrow 4 \Rightarrow \geq 0$$

$$\therefore (1, 2) \cup (3, \infty)$$



Solve & Graph the solution set.

$$\frac{x^2 + 8x + 12}{x^2 - 16} > 0$$

Polyn'1 & Rat. Ineq

400

$$\frac{x^2 + 8x + 12}{x^2 - 16} > 0$$

Critical Points: -4, 2, 4, 6

Intervals:

$$(-\infty, -4) \Rightarrow -5 \Rightarrow > 0$$

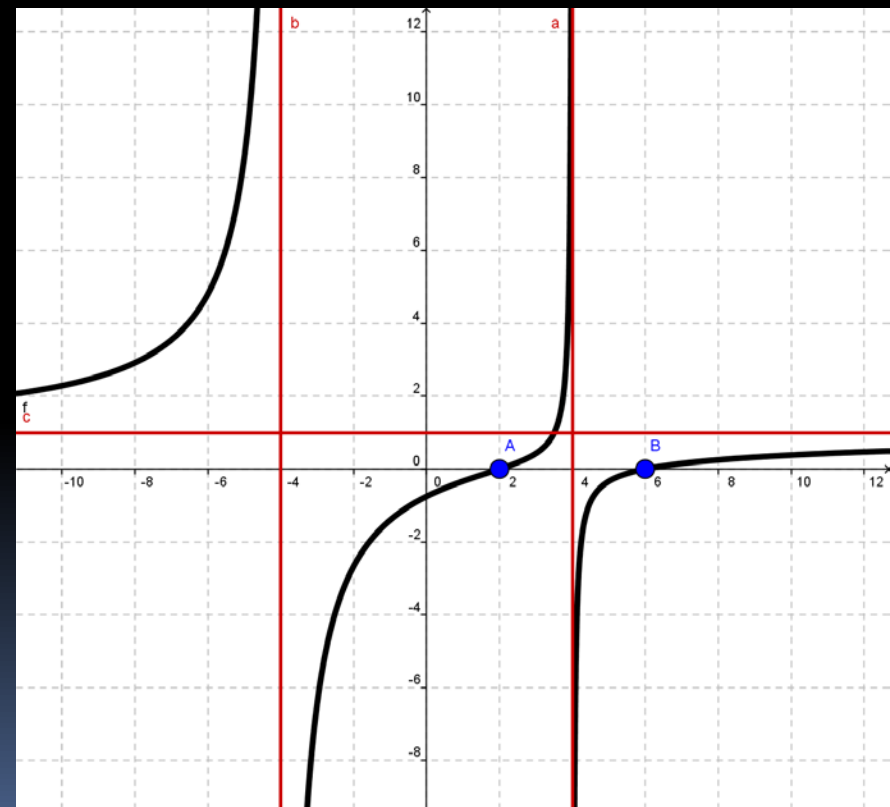
$$(-4, 2) \Rightarrow 0 \Rightarrow < 0$$

$$(2, 4) \Rightarrow 3 \Rightarrow > 0$$

$$(4, 6) \Rightarrow 5 \Rightarrow < 0$$

$$(6, \infty) \Rightarrow 7 \Rightarrow > 0$$

$$\therefore (-\infty, -4) \cup (2, 4) \cup (6, \infty)$$



Solve & Graph the solution set.

$$\frac{x(x^2 + x - 2)}{x^2 + 9x + 20} \leq 0$$

Polyn'l & Rat. Ineq

500

$$\frac{x(x^2 + x - 2)}{x^2 + 9x + 20} \leq 0$$

Critical Points: -5, -4, -2, 0, 1,

Intervals:

$$(-\infty, -5) \Rightarrow -6 \Rightarrow \leq 0$$

$$(-5, -4) \Rightarrow -4.5 \Rightarrow \geq 0$$

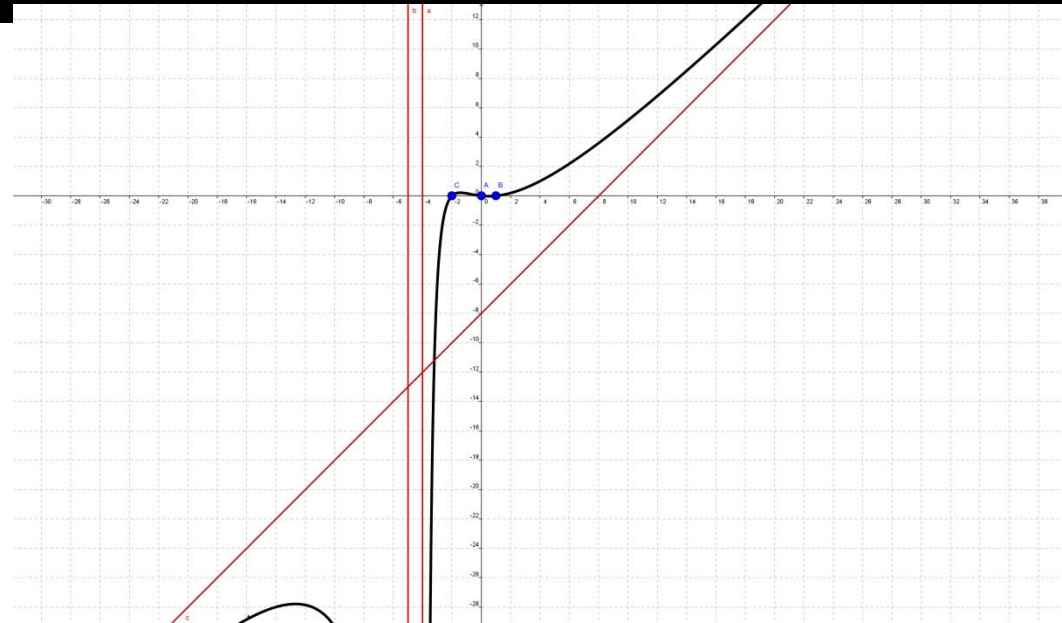
$$(-4, -2) \Rightarrow -3 \Rightarrow \leq 0$$

$$(-2, 0) \Rightarrow -1 \Rightarrow \geq 0$$

$$(0, 1) \Rightarrow 0.5 \Rightarrow \leq 0$$

$$(1, \infty) \Rightarrow 2 \Rightarrow \geq 0$$

$$\therefore (-\infty, -5) \cup (-4, -2) \cup (0, 1)$$



Find the equation of the line in slope-intercept form for a line that has slope -2 and contains the point $(3, -1)$.

Grab Bag

100

$$m = -2, \text{ contains } (3, -1)$$

pt - slope :

$$y + 1 = -2(x - 3)$$

$$y = -2x + 6 - 1$$

$$y = -2x + 5$$

Find the difference quotient of $y = x^3$

Grab Bag

200

$$f(x) = x^3$$

$$\begin{aligned} D.Q. &= \frac{f(x+h) - f(x)}{h} = \frac{(x+h)^3 - x^3}{h} = \frac{x^3 + 3x^2h + 3xh^2 + h^3 - x^3}{h} \\ &= 3x^2 + 3xh + h^2 \end{aligned}$$

Find all values of x

$$\sqrt{12 - x} = (2^{\frac{3}{2}})x$$

$$(\sqrt{12-x})^2 = ((2^{\frac{3}{2}})x)^2$$

$$12-x = 8x^2$$

$$8x^2 + x - 12 = 0$$

$$x = \frac{-1 \pm \sqrt{1+384}}{16} = \frac{-1 \pm \sqrt{385}}{16}$$

Find the Quotient and the Remainder

$$\frac{3x^5 - x^2 + x - 2}{3x^3 - 1}$$

Grab Bag

400

Use Long/Synthetic Division on:

$$\frac{3x^5 + 0x^4 + 0x^3 - x^2 + x - 2}{3x^3 + 0x^2 + 0x - 1}$$
$$= x^2 + \frac{x - 2}{3x^3 - 1}$$

A candy store sells boxes of candy containing caramels and crèmes. Each box sells for \$12.50 and holds 30 pieces of candy (all pieces are the same size). If the caramels cost \$0.25 to produce and the crèmes cost \$0.45 to produce, how many of each should be in a box to make a profit of \$3?

Grab Bag

500

Let x be the number of caramels, y be the number of cremes.

$$x + y = 30$$

$$x = 30 - y$$

$$0.25x + 0.45y = 12.50$$

$$0.25(30 - y) + 0.45y = 12.50$$

$$7.5 + 0.2y = 12.50$$

$$y = 10, \Rightarrow x = 20$$